

*Jr. of Industrial Pollution Control 31(1)(2015) pp 41-45*  
© EM International  
Printed in India. All rights reserved  
www.envirobiotechjournals.com

## OPTIMIZATION OF PID CONTROLLER PARAMETERS FOR SO<sub>2</sub> EMISSION CONTROL PROCESS USING PSO ALGORITHM

C. MAHESWAR<sup>1</sup>, S.R. ARUN<sup>1</sup>, V.MAGALINGAM<sup>1</sup>, K. JEEVANRAJ<sup>1</sup> AND K. KRISHNAMURTHY<sup>2</sup>

<sup>1</sup> Department of Mechatronics Engineering, School of Building and Mechanical Sciences,  
Kongu Engineering College, Perundurai, Tamil Nadu, India.

<sup>2</sup> School of Building and Mechanical Sciences, Kongu Engineering College, Perundurai, Tamil Nadu, India.

(Received 15 March, 2014; accepted 30 April, 2014)

**Key words :** SO<sub>2</sub>, Emission, PSO algorithm, Air quality

### ABSTRACT

This paper presents the application of PID controller for SO<sub>2</sub> emission control process using Particle Swarm Optimization (PSO) algorithm. To minimize the impacts of SO<sub>2</sub>, it must be removed from flue gas. Zeiglar-Nichols based PID (ZN-PID) controller is developed for SO<sub>2</sub> emission control process using MATLAB/SIMULINK platform. Based on the tuning parameters of ZN-PID controller, optimization of PID controller parameters are obtained based on PSO algorithm. Performance of the PSO based PID controller is analysed and compared with Ziegler-Nichols PID controller (ZN-PID) and IMC controller in terms of time domain performance measures such as settling time and rise time ( $t_s$  and  $t_r$ ) and error indices (ISE, IAE, ITAE). The simulation results proved that the PSO-PID controller provides most consistent performance as compared to the conventional controllers.

### INTRODUCTION

SO<sub>2</sub> is the major atmospheric pollutant resulted from combustion of coal and oil. The main sources of SO<sub>2</sub> emissions are coal fired boilers, sulphuric acid plants, chemical and metallurgical furnaces. Many techniques have been proposed for SO<sub>2</sub> removal process such as wet flue gas desulphurization, dry flue gas desulphurization and semi dry flue gas desulphurization techniques (Yuegui Zhou *et al.*, 2009). Among all the techniques, wet type flue gas desulphurization produces more removal efficiency (Cofalaa *et al.*, 2004).

While considering the absorbent to the wet FGD process, lime stone based flue gas desulphurization

technique is most widely used since it gives more than 90% removal efficiency but it produces CO<sub>2</sub> as a secondary emission to the atmosphere (Edward *et al.*, 2004). Based on the results given in Colle *et al.* (2005), the flow rate and concentration of hydrogen peroxide has the direct influence on outlet SO<sub>2</sub> concentration. For regulating the flow rate of hydrogen peroxide, an appropriate controller is required to improve the removal efficiency by reducing outlet SO<sub>2</sub> concentration.

Zeiglar and Nichols (1949) developed simple and robust tuning rule which is a widely practiced conventional control technique in many industrial applications. Skogestad (2003) developed model based

\* Corresponding author's email : arun.suresh208@gmail.com

tuning algorithm called as Internal model Controller (IMC) proved that it provides better control action since it is designed based on the transfer function model of the process.

PSO is an evolutionary-type global optimization algorithm (Kennedy & Eberhart, 1995) which is different from well-known similar algorithms in that no operators, inspired by evolutionary procedures, are applied to the population to generate new promising solutions. PSO has already been used to determine optimal solution to several power engineering problems such as reactive power and voltage control (Yoshida *et al.*, 2000) and state estimation (Naka *et al.*, 2001).

The present work focussed on tuning the PID controller using PSO algorithm. The PSO-PID controller is simulated within various scenarios and its performance is compared with those of an optimally designed PID controller.

### Particle Swarm Optimization (PSO)

PSO is a population based evolutionary algorithm that was developed from research on swarm such as fish schooling and bird flocking (Kennedy & Eberhart, 1995). PSO is a robust stochastic optimization technique based on the movement and intelligence of swarms. PSO applies the concept of social interaction to problem solving. It uses a number of agents (particles) that constitute a swarm moving around in the search space looking for the best solution.

Let the swarm consists of  $N$  particles moving around in a search space. Each swarm is initialized with a random position and velocity. Based on its own and companions experience at every iteration each particle modifies its position and velocity. The  $i$ th particle is denoted by  $X_i = (x_{i1}, x_{i2}, \dots, x_{in})$  and its individual best previous value (pbest) is represented as  $P_i = (p_{i1}, p_{i2}, \dots, p_{in})$ . Current velocity is given by  $V_i = (v_{i1}, v_{i2}, \dots, v_{in})$ . Finally, the overall best solution achieved by the whole swarm (gbest) is represented as  $P_g = (p_{g1}, p_{g2}, \dots, p_{gn})$ . The fitness function evaluates the performance of particles to determine whether the best fitting solution is achieved. The particles are modified based on the following equations:

$$v_{in}^{new} = w_i v_{in}^{old} + c_1 (p_{in} - x_{in}) + c_2 (p_{gn} - x_{in}) \quad (1)$$

$$x_{in}^{new} = x_{in}^{old} + v_{in}^{new} \quad (2)$$

Where,  $c_1$  and  $c_2$  are two positive constants and  $w$  is the inertia factor

$w$  balances the global wide-range exploitation and the local nearby exploration abilities of the swarm and is given by

$$w = w_{max} - \left[ \frac{(w_{max} - w_{min})}{iter_{max}} \right] * iter \quad (3)$$

Where,  $iter_{max}$  is the maximum number of iterations and  $iter$  is the current number of iterations.

## MATERIALS AND METHODS

### Modelling of SO<sub>2</sub> Emission Control Process

Absorption is the process of converting a gaseous pollutant from gas phase to a liquid phase. It involves the removal of gaseous pollutants by making them to dissolve in a liquid (Sinnott 1991). For this process, packed column is designed based on the principle of gas-liquid interface to obtain proper liquid to gas mixing. It leads to the efficient removal of soluble SO<sub>2</sub> from gas stream.

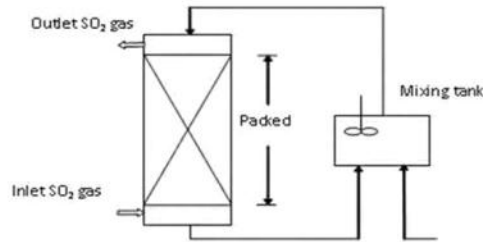


Fig. 1 Schematic of control setup

Figure 1 illustrates the schematic of control set up used for SO<sub>2</sub> emission control process. Packed column (or) liquid-gas absorption column is used for analysis. Flue gas with maximum of 5000 ppm SO<sub>2</sub> concentration is entered at the inlet of the packed column. The mixing tank containing fresh hydrogen peroxide is flowing towards the top of the column. The flow rate of hydrogen peroxide has the direct influence on the SO<sub>2</sub> absorption rate. Hence based on the concentration of SO<sub>2</sub> leaving out of the column, flow rate of SO<sub>2</sub> is manipulated to get better SO<sub>2</sub> removal efficiency.

Mathematical modelling is developed by considering material balance equations and reaction of kinetics of SO<sub>2</sub> removal process. Detailed mass balance study is carried out based on the material balance and kinetic chemical equations for Figure 1.

MATLAB/SIMULINK model is developed based on Figure 1. Open loop response is identified for flow rate of hydrogen peroxide Vs SO<sub>2</sub> removal efficiency. From the open loop response, the process is approximated to first order plus time delay (FOPTD) transfer function shown in equation 1.

$$G(s) = \frac{K_z}{\tau_z s + 1} e^{-tds} \quad (4)$$

Based on open loop response graph, the model parameters K<sub>p</sub>, and t<sub>p</sub> are identified by step test method. The worst case model is selected and the identified transfer function is given by,

$$G(s) = \frac{27}{244s + 1} e^{-1s} \quad (5)$$

A PID controller has proportional, integral and derivative terms that can be represented in transfer function form as

$$K(s) = K_p + \frac{K_i}{s} + K_d s \quad (6)$$

#### Performances Criteria

Different tuning rules are used to calculate the parameters of PID controller. Probing the optimal parameters of PID controller is an optimum problem in essence. PSO technique is used to determine the optimal values of the PID controller in this paper. There are several performance criterions for design of controllers. Integral of absolute error (IAE), integral of squared error (ISE) and integral of time-weighted-squared-error (ITSE) are often used in literatures to design controllers. Gaing (2004), illustrated that the performance criterion  $w(z)$  is defined for PID controller design, is defined as

$$W(z) = (1 - e^{\beta}) * (M_p + E_{ss}) + e^{\beta} * (t_s - t_r) \quad (7)$$

where  $\beta$  is a weighting factor,  $M_p$ ,  $E_{ss}$ ,  $t_r$  and  $t_s$  are respectively the overshoot, steady-state error, rising time and settling time.

#### Design process of PSO-PID

The design process of PSO based PID controller for SO<sub>2</sub> emission controller process is summarized as follow:

- Initialize the parameters like number of iteration and particle size
- Randomly initializing swarm velocities and position
- For each initial particle of the population, calculate the values of the performance criterion
- Compare each particles evaluation values and calculate personal best position  $P_i(t)$  and global best position  $P_g(t)$
- Update swarm position and velocity based on the eqn
- If the number of iteration reaches the maximum value evaluate  $P_g$  which is the optimal controller parameter else goto step (iii)

The optimized parameters of the PID controller based on PSO algorithm are  $K_p = 0.05776$ ,  $K_i = 0.00038$  and  $K_d = 0.29905$ .

#### RESULTS AND DISCUSSION

The MATLAB/SIMULINK platform is developed for the SO<sub>2</sub> emission control process. Tuning values that are optimized using PSO algorithm is used to control the process. Response of the PSO-PID, IMC-PID and ZN-PID for 500 ppm operating point is shown in Figure 2. The figure clearly shows that PSO-PID gives better performances than ZN-PID and IMC-PID controller and it is ensured with the performance measures in terms of error indices Integral Squared Error (ISE), Integral Absolute Error (IAE), Integral Time Absolute Error (ITAE), and Quality indices (rise time  $t_r$ , settling time  $t_s$ ) of the controller. the performance measures tabulated in Table 1 shows that PSO-PID controller provides less error indices and good quality indices.

Further, the performance of the controller is verified with the disturbance test. It is obtained by changing set point from 500 ppm SO<sub>2</sub> outlet concen-

**Table 1.** Performance measures of PSO-PID, ZN-PID and IMC-PID controller

Controller	ISE	IAE	ITAE	Rise Time ( $t_r$ ) (Sec)	Settling Time ( $t_s$ ) (Sec)
ZN-PID	54.84*10 <sup>7</sup>	27.29*10 <sup>4</sup>	23.42*10 <sup>6</sup>	58	1025
IMC-PID	42.04*10 <sup>7</sup>	16.98*10 <sup>4</sup>	68.01*10 <sup>5</sup>	76	813
PSO-PID	25.69*10 <sup>7</sup>	94.63*10 <sup>3</sup>	17.19*10 <sup>5</sup>	53	500



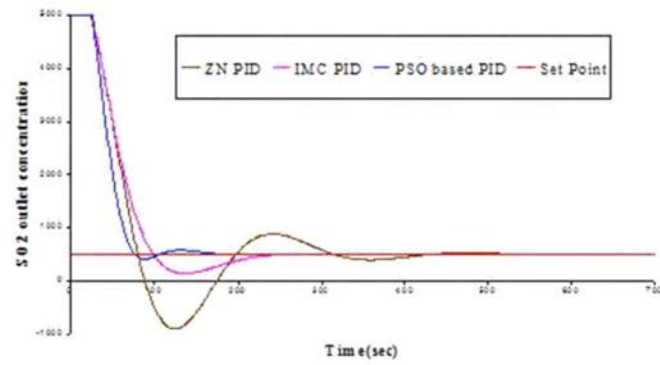


Fig. 2 Performance of PSO-PID, ZN-PID and IMC-PID controller

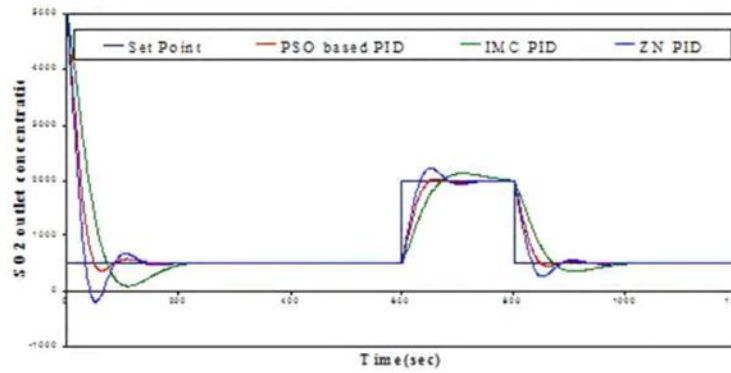


Fig. 3 Disturbance rejection test on ZN-PID, IMC-PID and PSO-PID

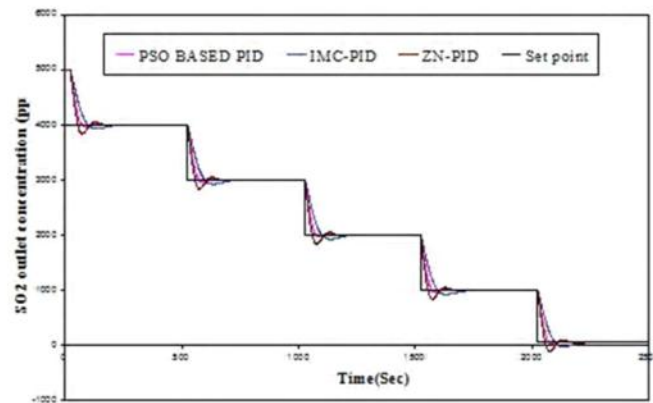


Fig. 4 Closed loop transient responses at different operating points

tration into 2000 ppm at 600 seconds, and it is maintained up to 800 sec as shown in Figure 3. The performance graph shows that the PSO-PID controller reaches the set point at the earliest than the conventional controllers.

The performance of the controllers are tested for different continuous tracking cases at 4000 ppm, 3000 ppm, 2000 ppm, 1000 ppm and 50 ppm SO<sub>2</sub> outlet concentrations as shown in Figure 4. The figure ensure that the better performance achieved by PSO-PID controller at all operating points.

## CONCLUSION

SO<sub>2</sub> emission control process is modelled using mathematical equations and based on the open loop response transfer function is determined. In order to implement a better control action over the SO<sub>2</sub> emission control process, PID controller parameters are optimized based on performance measures. The PSO based PID controller parameters are calculated ( $K_p = 0.05776$ ,  $K_i = 0.00038$  and  $K_d = 0.29905$ ) and its performance is compared with the conventional controllers such as ZN-PID and IMC-PID controllers. The simulation results developed in MATLAB/SIMULINK platform ensured that the optimized tuning parameters provide better control action over the conventional controllers.

## REFERENCES

- Cofalaa, J., Amanna, M., Gyarfasa, F., Schoeppa, W., Boudrib, J.C., Hordijka, L., Kroezeb, C., Junfengc, L., Linc, D., Panward, T.S. and Guptad, S. 2004. Cost effective control of SO<sub>2</sub> emission in Asia. *Journal of Environment Management*. 57 : 149-161.
- Colle, S., Thomas, D. and Vanderschuren, J. 2005. Process simulation of sulphur Dioxide abatement with H<sub>2</sub>O<sub>2</sub> solutions in a packed column. *Chemical Engineering and Design*. 83 (A1) : 81-87.
- Gaing, Z.L. 2004. A particle swarm optimization approach for optimum design of PID controller in AVR system. *IEEE Transactions on Energy Conversion*. 19 : 384-391.
- Kennedy, J. and Eberhart, R. 1995. Particle swarm optimization. In *Proceedings of IEEE International Conference on Neural Networks*. 4 : 1942-1947.
- Naka, S., Genji, T., Yura, T. and Fukuyama, Y. 2001. Practical distribution state estimation using hybrid particle swarm optimization. In *Proceedings of IEEE Power Engineering Society*. 2 : 815-820.
- Sinnott, R.K. 1991. *Coulson and Richardson's Chemical Engineering Design*, Jordan Hill, Oxford, ISBN: 0750665386.
- Skogestad, S. 2003. Simple analytic rules for model reduction and PID controller tuning. *Journal of Process Control*. 13 : 291-309.
- Yoshida, H., Kawata, K. and Fukuyama, Y. 2000. A particle swarm optimization for reactive power and voltage control considering voltage security assessment. *IEEE Transactions on Power Systems*. 15 (4) : 1232-1239.
- Yuegui Zhou, Xian Zhu, Jun Peng, Yaobin Liu, Dingwang Zhang and Mingchuan Zhang, 2009. The effect of hydrogen peroxide solution on SO<sub>2</sub> removal in the semidry flue gas desulfurization process. *Journal of Hazardous Materials*. 170 (1) : 436- 442.
- Zeigler, J.G. and Nichols, N.B. 1942. *Optimum Settings for Automatic Controllers*. 2 : 125.