

TEMPERATURE TREND ANALYSIS USING NONPARAMETRIC TEST: A CASE STUDY OF COIMBATORE CITY

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ABSTRACT

Livelihoods of people, socio economic development and biodiversity as a whole are affected due to rise in temperature. In this study temperature trend analysis is studied for the Coimbatore district, which witnessed a speedy industrial and business growth from the 1920s. Well established nonparametric tests like Mann-Kendall, Sen's slope and Pettitt's test are applied to the maximum and minimum temperatures to find the nature of trend and detect the change point. The result of the analysis confirmed an increasing trend in both minimum and maximum temperatures in all the months and seasons post 1950.

INTRODUCTION

Population growth, industrialization, and global warming are the root cause for rise in temperatures (IPCC, 2013; Rao, *et al.*, 2016). There has been a drastic change in global climatic conditions in recent years. Global land evapotranspiration influence the variation in land precipitation (Qian, *et al.*, 2006) which results in frequent extreme weather events and risks (Briffa, *et al.*, 2009; Vasiliades, *et al.*, 2009). Many have studied and analyzed the trends in long term temperature, its interannual, seasonal and decadal variability by using different nonparametric tests (Bhutiya, *et al.*, 2008; Jaiswal, *et al.*, 2015; Jagannathan and Parthasarathy, 1973; Xavier, 2006; Wijngaard, *et al.*, 2003). Though various statistical methods are employed by researchers for analyzing trends and change point detection, nonparametric methods are preferred over parametric ones. Since parametric tests are mostly appropriate for normally distributed data, if the assumed data distribution deviates considerably from the standard, then

the nonparametric test gives much better results than the parametric one (Hirsch, *et al.*, 1992; Pettitt, 1979). In this study, the trend and change point detection is examined for the minimum and maximum temperature series of Coimbatore district by employing different nonparametric tests. Mann-Kendall's test and Sen's slope test are used for trend analysis and Pettitt's test is employed for change point detection.

STUDY AREA

Coimbatore district is situated in the northwestern part of Tamil Nadu. It lies between 10°13'4" North and 11° 24'5" North latitudes and 76°39'25" East and 77°18'26" East longitudes. It is one among the industrially developed and commercially vibrant districts of Tamil Nadu. The district is situated on the banks of river Noyyal, a tributary of the river Cauvery and is bounded by Tiruppur district in the east, Nilgiris district in the north, Erode district in the northeast, Palghat district and Idukki district of the neighboring state of Kerala in the west and south,

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respectively. The gradient of the district decreases gradually from west to east. The district was bifurcated into Coimbatore and Erode districts in the year 1979 and presently it consists of two revenue divisions and six taluks. It has a high concentration of small, medium and large scale industries. It is also called as the Manchester of South India because of its well-developed textile, commerce and other industrial areas. The district gained an economic boom between the years 1920 and 1930 due to decline of cotton industry in Mumbai (Dhanalakshmi and Priyatharsini; 2015; www.coimbatore.nic.in) (Fig. 1).

Box plot showing the characteristics of minimum and maximum temperatures is presented in (Fig. 2 and Fig. 3).

METHODOLOGY

Mann-Kendall's Test

The nonparametric Mann-Kendall test is commonly employed to detect monotonic trends in series of environmental data, climate data or hydrological data. The null hypothesis, H_0 , is that the data come from a population with independent realizations and are identically distributed. The alternative hypothesis, H_A , is that the data follow a monotonic

trend (Karmeshu, 2012; Libiseller and Grimvall, 2002; Menne and Williams, 2005). The Mann-Kendall test statistic is calculated according to:

$$S = \sum_{i=1}^n \sum_{j=1}^{i-1} \text{sign}(x_i - x_j) \quad (1)$$

where n is the total length of data, x_i and x_j are two generic sequential data values, and function $\text{sign}(x_i - x_j)$ assumes the following values

$$\text{sign}(x_i - x_j) = \begin{cases} 1, & \text{if } (x_i - x_j) > 0 \\ 0, & \text{if } (x_i - x_j) = 0 \\ -1, & \text{if } (x_i - x_j) < 0 \end{cases} \quad (2)$$

Pettitt's Test

The approach after Pettitt is commonly applied to detect a single change-point in hydrological series or climate series with continuous data. It tests the H_0 : The T variables follow one or more distributions that have the same location parameter (no change), against the alternative: a change point exists (Dhanalakshmi and Priyatharsini, 2015; Menne and Williams, 2005). The non-parametric statistic is defined as:

$$K_T = \max |U_t| \quad (3)$$

Where

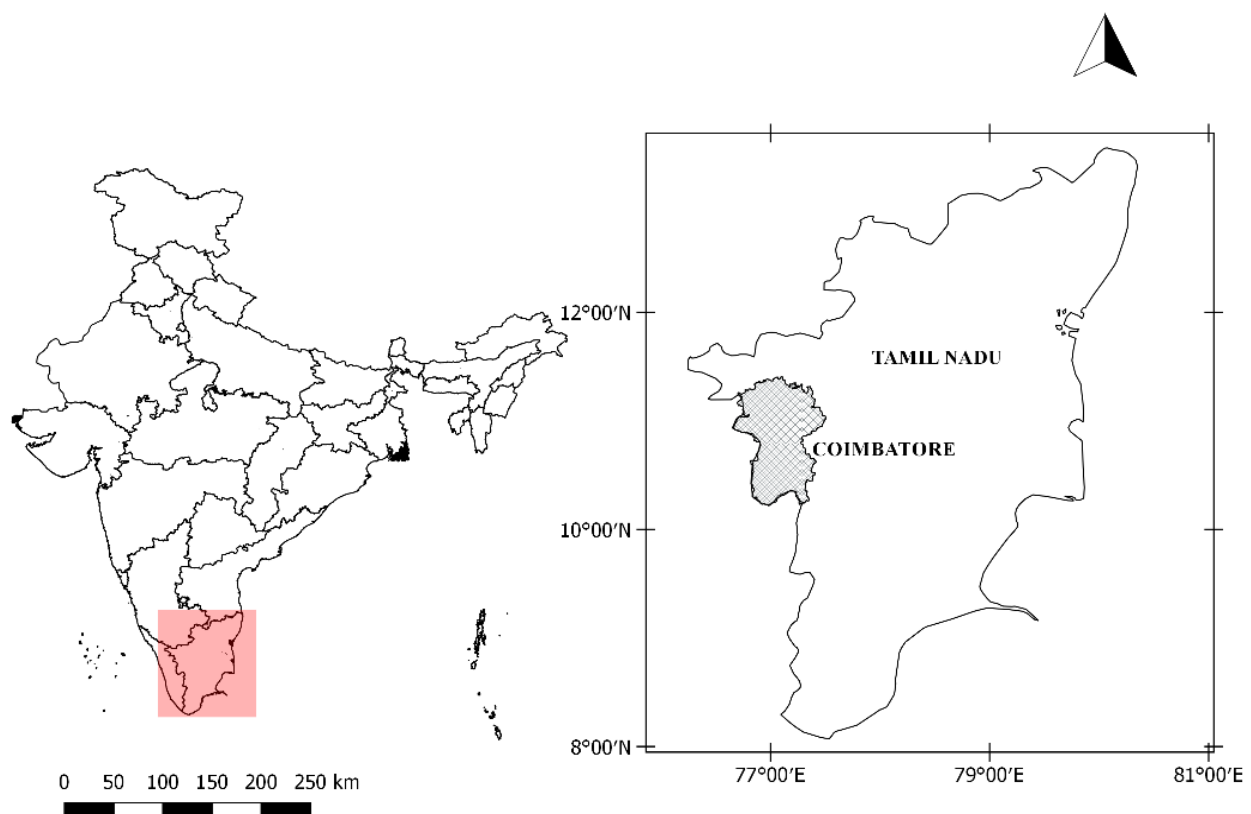


Fig. 1 Location map of Coimbatore district, Tamil Nadu, India.

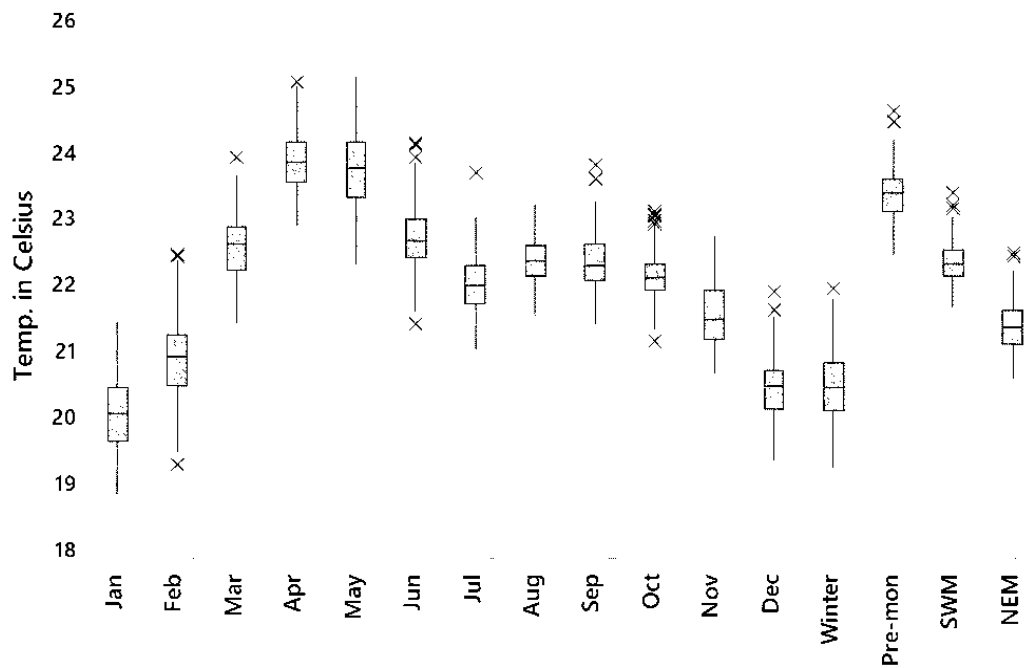


Fig. 2 Box plot of monthly minimum temperatures averaged over years.

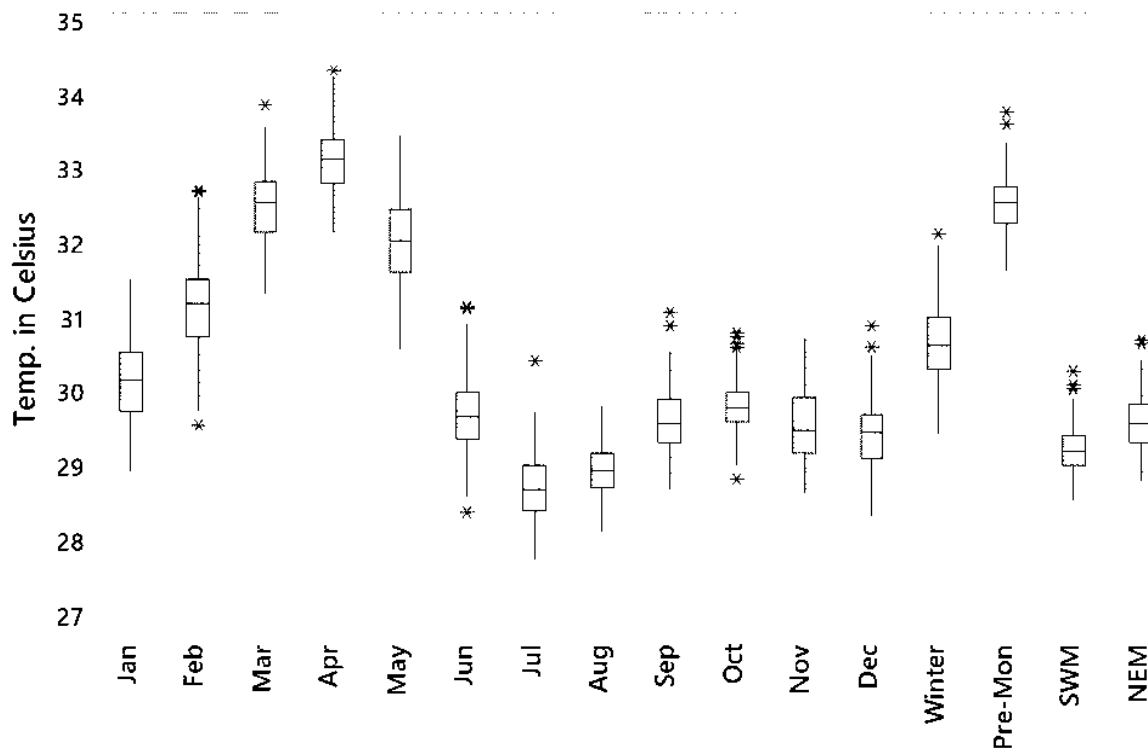


Fig. 3 Box plot of monthly maximum temperatures averaged over years.

$$U_i = \sum_{t=1}^i \sum_{j=t+1}^n \text{sign}(x_t - x_j)$$

$$\text{sign}(x_i - x_j) = \begin{cases} 1, & \text{if } (x_i - x_j) > 0 \\ 0, & \text{if } (x_i - x_j) = 0 \\ -1, & \text{if } (x_i - x_j) < 0 \end{cases}$$

- (4) The test statistic counts the number of times a member of the first sample exceeds the member of second sample. The null hypothesis of the Pettitt's test is the absence of a change point.

(5) Sen's Slope Test

This test computes both the slope (i.e., linear rate of

change) and intercept according to Sen's method. First, a set of linear slopes is calculated as follows:

$$T_i = \frac{x_j - x_k}{j - k} \text{ where } i=1, 2, 3, \dots, N \text{ and } j > k \quad (6)$$

where $x_1, x_2, x_3, \dots, x_j, x_k, \dots, x_n$ are the data values and the median of N values of T_i series can be obtained as Sen's estimator of slope (Libiseller and Grimvall, 2002).

ANALYSIS OF RESULTS

Detection of trend

The monthly temperature data from 1902–2002 is obtained from the Indian Meteorological Department (IMD) site India Water Portal (<http://www.indiawaterportal.org/metdata>) (Mitchell, *et al.*, 2004) and the seasonal classification for the analysis was followed as per Indian Meteorological Department (IMD) viz. winter (January–February), summer (March–May), southwest monsoon (June–September) and northeast monsoon (October–December). For the determination of trend, Mann-Kendall's test has been applied on the data series of maximum and minimum temperatures. The trend is detected based on the z value at the given significance level. If the z value is greater than the significance level, the null hypothesis (H_0) is rejected and the rejection of H_0 indicates that there is a trend in the time series. The results of Mann-Kendall test statistic is presented in Table 1. The test results showed significant increasing trend in both maximum and minimum temperatures in all the months and seasons barring August.

To determine the change point for the maximum and minimum temperature series, Pettitt's test has been applied. The results are presented in Table 2. It is observed that the change point of minimum and maximum temperature series of all the months and seasons varies between the years 1950 and 1980. A number of trial runs were performed to find the exact change point by dividing the entire span with respect to the results obtained in Table 2. Based on the test outcomes, the entire span of 1902–2002 (P-1) is divided into two periods viz. P-2 (1902–1951) and P-3 (1941–2002) for which trend analysis is performed again to substantiate the change point.

Mann-Kendall's test results for P-2 and P-3 are presented in Table 3 and Table 4. For the minimum temperature series (Table 3), P-2 (1902–1951) period shows significant trend for January and April and no significant trend is identified for the other months and seasons. For the period P-3 (1941–2002), an upward trend is witnessed for all the months and seasons. An increasing trend is also witnessed for the maximum temperature series for the period P-3 (Table 4). Thus the trend analysis confirmed a significant rising trend in all monthly and seasonal series during the period 1941–2002 (P-3). The significant increase in temperature might be due to the growth of industrialization in Coimbatore district post 1930s. The annual series of minimum and maximum temperatures when plotted and fitted linearly showed that both series exhibited strong rising trend during the period P-3, while an insignificant trend was detected in P-2 (Fig. 4).

Table 1. Results of Mann Kendall test statistics (Z) during 1902–2002

Period	Minimum Temperature		Maximum Temperature	
	Z	Type of trend	Z	Type of trend
January	5.90	Positive	5.86	Positive
February	5.62	Positive	5.61	Positive
March	5.17	Positive	5.19	Positive
April	2.54	Positive	2.47	Positive
May	1.98	Positive	2.00	Positive
June	2.92	Positive	2.92	Positive
July	2.61	Positive	2.56	Positive
August	1.07	-	1.08	-
September	2.87	Positive	2.87	Positive
October	3.33	Positive	3.38	Positive
November	6.01	Positive	6.19	Positive
December	6.02	Positive	6.24	Positive
Annual	6.04	Positive	6.08	Positive
Winter	6.51	Positive	6.49	Positive
Pre-Mon	3.91	Positive	3.88	Positive
SWM	3.20	Positive	3.22	Positive
NEM	6.57	Positive	6.53	Positive

Table 2. Results of change point analysis

Period	Minimum temperature			Maximum temperature		
	Pettitt's Statistics	Shift	Year of Shift	Pettitt's Statistics	Shift	Year of Shift
January	1463	Yes	1952	1455	Yes	1950
February	1521	Yes	1953	1519	Yes	1953
March	1368	Yes	1948	1363	Yes	1948
April	1041	Yes	1971	1037	Yes	1971
May	917	Yes	1982	918	Yes	1982
June	926	Yes	1981	928	Yes	1956
July	1300	Yes	1981	1289	Yes	1981
August	883	No	-	887	No	-
September	1186	Yes	1981	1184	Yes	1981
October	1364	Yes	1975	1377	Yes	1975
November	1645	Yes	1973	1647	Yes	1975
December	1715	Yes	1956	1724	Yes	1956
Annual	1622	Yes	1981	1622	Yes	1981
Winter	1639	No	-	1640	Yes	1951
Pre-Mon	1273	Yes	1972	1972	Yes	1972
SWM	1414	Yes	1981	1416	Yes	1981
NEM	1758	Yes	1975	1760	Yes	1975

Table 3. Mann-Kendall's test and trends in different periods of minimum temperature

Period	1902-1951		1941-2002	
	Test Statistics	Trend	Test Statistics	Trend
January	1.70	Upward	3.76	Upward
February	0.43	-	4.15	Upward
March	0.69	-	3.31	Upward
April	-2.36	Downward	3.46	Upward
May	0.60	-	1.66	Upward
June	-1.05	-	2.79	Upward
July	-1.27	-	3.87	Upward
August	-0.94	-	2.17	Upward
September	-0.84	-	4.35	Upward
October	0.04	-	3.72	Upward
November	0.45	-	5.56	Upward
December	1.15	-	4.27	Upward
Annual	0.02	-	5.24	Upward
Winter	1.47	-	4.29	Upward
Pre-Mon	-0.55	-	3.54	Upward
SWM	-1.18	-	4.24	Upward
NEM	0.75	-	5.70	Upward

Sens's Slope Estimator Test

Sen's slope was computed to know the prevailing trends in monthly and seasonal series of minimum and maximum temperatures. The Sen's slope parameters for minimum and maximum temperature series are presented in Table 5. The analysis of Sen's slope estimator clearly indicated a positive trend in P-3 (1941-2002) period for both maximum and

minimum temperature series while the same was either negative or with a minimal positive value in P-2 (1902-1950).

CONCLUSION

Rapid industrialization, global warming and other meteorological factors play a significant role in the rise in temperature. This has an apparent effect globally which might be in the form of increased

Table 4. Mann-Kendall's test and trend in different periods of maximum temperature

Period	1902-1951		1941-2002	
	Test Statistics Statistic	Trend	Test Statistics	Trend
January	1.50	-	4.00	Upward
February	0.53	-	4.40	Upward
March	0.54	-	3.57	Upward
April	-2.25	Downward	3.56	Upward
May	0.53	-	1.78	Upward
June	-0.75	-	2.75	Upward
July	-1.13	-	3.87	Upward
August	-1.21	-	2.33	Upward
September	-1.22	-	4.10	Upward
October	-0.24	-	3.48	Upward
November	0.11	-	5.68	Upward
December	0.11	-	4.35	Upward
Annual	-0.18	-	5.42	Upward
Winter	1.52	-	4.59	Upward
Pre-Mon	-0.51	-	3.78	Upward
SWM	-1.20	-	4.20	Upward
NEM	0.37	-	5.63	Upward

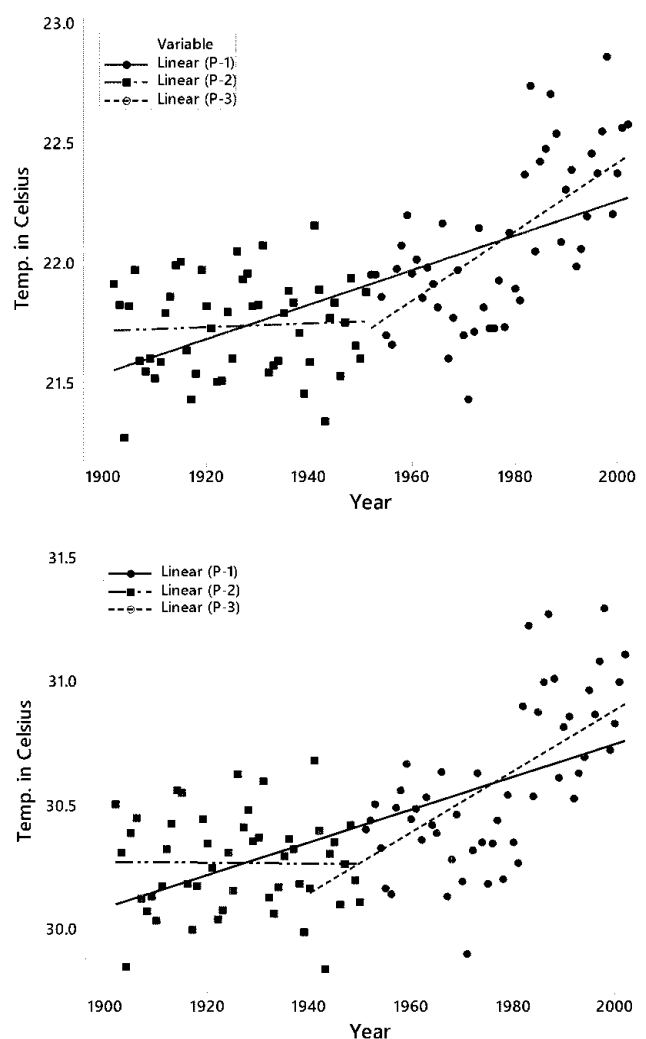


Fig. 4 Fitting of linear trends in minimum and maximum temperature series.

Table 5. Sen's Slope for minimum and maximum temperature

Period	Minimum Temperature		Maximum Temperature	
	1902-1950	1941-2002	1902-1950	1941-2002
January	0.008	0.0137	0.0082	0.0148
February	0.014	0.0138	0.0017	0.0146
March	0.030	0.0109	0.0027	0.0117
April	-0.011	0.0117	-0.0113	0.0118
May	-0.030	0.0070	0.0026	0.0069
June	-0.004	0.0104	-0.003	0.0099
July	-0.004	0.0125	-0.0038	0.0124
August	-0.003	0.0061	-0.0043	0.0063
September	-0.003	0.0140	-0.0053	0.0125
October	0	0.0113	-0.0006	0.0105
November	0.002	0.0192	0.0002	0.0189
December	0.006	0.0130	0.0061	0.0128
Annual	-0.0008	0.1416	-0.0038	0.1414
Winter	0.0136	0.0294	0.0143	0.0311
Pre-Mon	-0.005	0.028	-0.0052	0.0292
SWM	-0.0127	0.0423	-0.0134	0.0408
NEM	0.0073	0.0429	0.0042	0.0418

precipitation rising sea level, retreating glaciers etc. In the present study, trend analysis was studied by applying Mann-Kendall's test and the change point was found by using Pettitt's test for the maximum and minimum temperature series of Coimbatore district. The result of trend analysis by Mann-Kendall and Sen's slope showed a positive trend in the minimum and maximum temperature series between 1902 and 2002. The period P-2 (1902-1950) witnessed an insignificant trend while period P-3 (1941-2002) showed significant rising trend in temperature. The increase in temperature after 1940 is also substantiated by the Sen's slope values. The increase in temperature might change the hydrological cycle which will eventually affect the crop production and agricultural activities. Analyses such as these will help in proper decision-making in water resources.

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